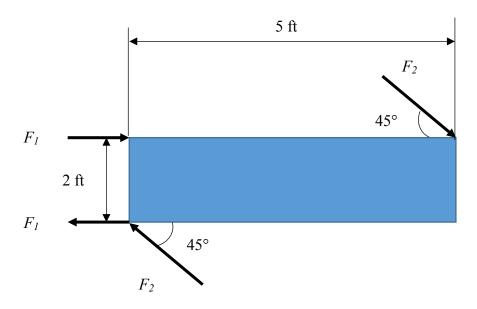
20. Two couples acting on the beam are independently and normally distributed with  $F_1 \sim N(250, 5^2)$  lb and  $F_2 \sim N(400, 3^2)$  lb. Determine the distribution of the resultant couple moment.



Solution

$$\mu_M = \mu_{F_1}(2) + \mu_{F_2} \cos 45^{\circ}(2) + \mu_{F_2} \sin 45^{\circ}(5) = 2479.9 \text{ lb} \cdot \text{ft}$$

$$\sigma_{M} = \sqrt{(2\sigma_{F_{1}})^{2} + (2\sigma_{F_{2}}\cos 45^{\circ})^{2} + (5\sigma_{F_{2}}\sin 45^{\circ})^{2}} = 15.2 \text{ lb} \cdot \text{ft}$$

Thus, the resultant moment is  $M \sim N(2479.9,15.2^2)$  lb·ft.