2. A load *W* follows a normal distribution $N(100,5^2)$ lb and is suspended from the hook. The load is supported by the cable *AD* lies in the *x*-*y* plane and cable *AC* lies in the *x*-*z* plane. The spring has a stiffness k = 400 lb/ft. Determine the distribution of the tension in the cables and the distribution of the stretch of the spring for equilibrium.



Solution



Equations of equilibrium

$$\sum F_{x} = 0; \ F_{D} \sin 45^{\circ} - \frac{3}{5}F_{C} = 0$$
$$\sum F_{y} = 0; \ -F_{D} \cos 45^{\circ} + F_{B} = 0$$
$$\sum F_{Z} = 0; \ \frac{4}{5}F_{C} - W = 0$$

We already know $W \sim N(100, 5^2)$ lb, and then we solve the above equations for the distribution of F_C

$$F_{c} = \frac{5}{4}W$$
$$\mu_{F_{c}} = \frac{5}{4}\mu_{W} = \frac{5}{4}(100) = 125 \text{ lb}$$
$$\sigma_{F_{c}} = \frac{5}{4}\sigma_{W} = \frac{5}{4}(5) = 6.25 \text{ lb}$$

So the distribution of the force in cable AC is $F_c \sim N(125, 6.25^2)$ lb. Ans.

Then the same for F_D , and finally F_B

$$F_D \sim N(106.07, 5.3^2)$$
 lb Ans.
 $F_B \sim N(75, 3.75^2)$ lb Ans.

The distribution of the stretch of the spring is therefore

$$F_B = kS_{AB}$$

$$S_{AB} = \frac{F_B}{k}$$

$$\mu_{S_{AB}} = \frac{\mu_{F_B}}{k} = \frac{75}{400} = 0.19 \text{ ft}$$

$$\sigma_{S_{AB}} = \frac{\sigma_{F_B}}{k} = \frac{3.75}{400} = 0.01 \text{ ft}$$

Thus, the distribution of the stretch of the spring is $S_{AB} \sim N(0.19, 0.01^2)$ ft . Ans.