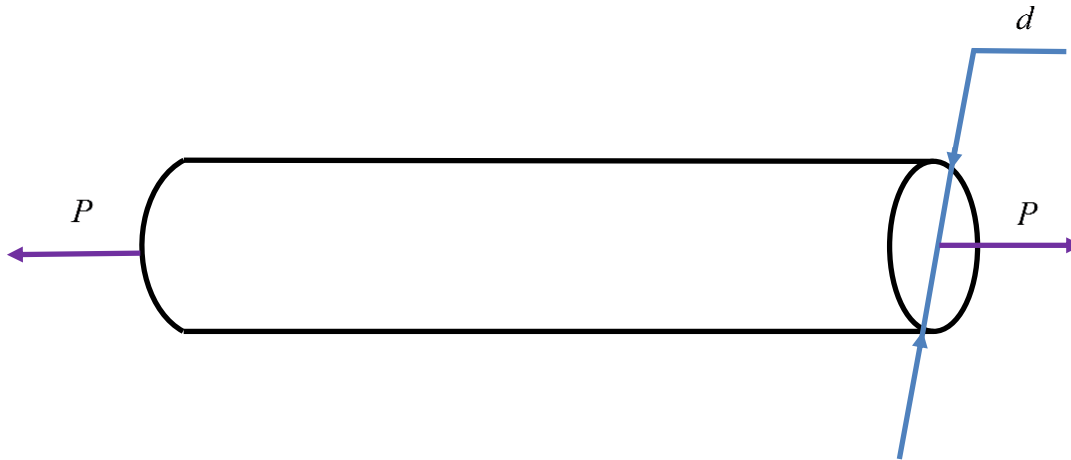


1. A solid circular rod is subjected to an axial force of  $P = 2000$  lbf . The yield stress of the rod is  $S_y = 20$  kpsi . The factor of safety is  $n_s = 3.0$  . a) What is the minimum diameter of the rod? Then select a preferred fractional diameter. b) If  $P \sim N(2000, 300^2)$  lbf ,  $S_y \sim N(20, 3^2)$  kpsi , and  $P$  and  $S$  are independent, determine the probability of failure using Monte Carlo Simulation.



### Solution

a) The cross-sectional area of the rod is

$$A = \frac{\pi}{4} d^2$$

The tensile stress of the rod is

$$S = \frac{P}{A} = \frac{4P}{\pi d^2}$$

The tensile stress should be less than the allowable stress

$$S = \frac{4P}{\pi d^2} \leq \frac{S_y}{n_s}$$

Solving for  $d$  yields

$$d \geq \sqrt{\frac{4Pn_s}{\pi S_y}} = \sqrt{\frac{4(2000)(3)}{\pi \times (20000)}} = 0.618 \text{ in}$$

Thus the minimum diameter of the rod is 0.618 in.

**Ans.**

And the preferred fractional diameter could be chosen as  $d_0 = \frac{5}{8} \text{ in} = 0.625 \text{ in}$ .

**Ans.**

- b) The limit-state function is the actual stress of the rod subtracted from the allowable maximum stress. Failure occurs when  $Y < 0$ .

$$Y = g(\mathbf{X}) = S_y - S = S_y - \frac{4P}{\pi d_0^2}$$

where  $\mathbf{X} = (P, S_y)$ , and  $d_0 = 0.625 \text{ in}$  is the preferred diameter.

Using Monte Carlo Simulation and  $1e7$  samples, the probability of failure is found to be  $1.16(10^{-5})$ .

**Ans.**