48. A torsion  $T \sim N(8, 0.8^2)$  kN·m is applied to a bar having a hollow round cross section with an inner diameter of  $d_i = 2$  cm. The allowable stress of the bar is  $\tau_a \sim N(20, 2^2)$  MPa. If the maximum probability of failure is designed to be  $p_f = 10^{-5}$ , determine the minimum outer diameter of the bar using the First Order Second Moment Method. Note that T and  $\tau_a$  are independent.

**Answer:**  $d_{min} = 157.7 \text{ mm}, d_{preferred} = 160 \text{ mm}$