55. A grinding wheel has a diameter of  $d_o = 200$  mm, and a bore with a diameter of  $d_i = 20$  mm. The weight of the wheel is  $m \sim N(1, 0.1^2)$  kg and the thickness is t = 5 mm. The Poisson's ration is v = 0.20. If the allowable tangential stress is  $S_a \sim N(3, 0.3^2)$  MPa and the maximum probability of failure is designed to be  $p_f = 10^{-5}$ , determine the maximum working speed of the grinding wheel using the theory of rotating rings.

Answer:  $n_{\text{max}} = 1917$  rpm