10. A ductile shaft is subjected to a toruqe  $T \sim N(800, 80^2)$  N·m. The yield strength in tension is  $S_{yt} \sim N(200, 20^2)$  MPa and the one in compression is  $S_{yc} \sim N(150, 10^2)$  MPa. If the maximum probability of failure is designed to be  $p_f = 10^{-5}$ , determine the minimum diameter of the shaft. Assume that T,  $S_{yt}$  and  $S_{yc}$  are independent.

Answer:  $d = 42.1 \text{ mm}, d_{preferred} = 45 \text{ mm}$