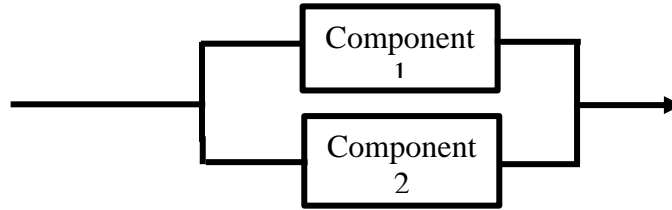


5. Two components of a system are in parallel. The reliability of component 1 is $R_1 = 0.99$, and the reliability of component 2 is $R_2 = 0.98$. If the failures of the two components are independent, find the probability that the system works.



Solution

- Event A = component 1 works
- Event B = component 2 works

$R_1 = P(A) = 0.99$; $R_2 = P(B) = 0.98$; A and B are independent

Let C = success of the system

$$\bar{C} = \bar{A}\bar{B}$$

$$R_s = 1 - P(\bar{C}) = 1 - P(\bar{A}\bar{B})$$

$$= 1 - P(\bar{A})P(\bar{B}) = 1 - (1 - R_1)(1 - R_2)$$

$$= 1 - (1 - 0.99)(1 - 0.98) = 0.9998$$

Notice: $R_s \geq R_1$, $R_s \geq R_2$, $R_s \geq \max(R_1, R_2)$