## **Homework 5 FOSM**

1. The limit-state function of a shaft in a speed reducer is defined by the difference between the strength and the maximum equivalent stress. It is given by

$$g(\mathbf{X}) = S - \frac{16}{\pi d^3} \sqrt{4F^2 l^2 + 3T^2}$$

where

- d = 39 mm, the diameter of the shaft
- l = 400 mm, the length of the shaft

F = the external force

T = the external torque

S = the yield strength



The distributions of the independent random variables are given below.

| Table 1 Distributions |         |        |              |
|-----------------------|---------|--------|--------------|
| Variables             | Mean    | Std    | Distribution |
| External force F      | 2000 N  | 220 N  | Normal       |
| Torque T              | 450 N∙m | 50 N·m | Normal       |
| Strength S            | 250 MPa | 30 MPa | Normal       |

Use FOSM to calculate the probability of failure.